temperature regime from (9), which joins smoothly to the second virial coefficient approximation for S in the high-temperature regime (20). The Fig. 3 inset shows the low-temperature behavior, which is about five times the string theory limit (Fig. 3, inset, red dashed line) near the critical energy $E_c/E_F = 0.7$ to 0.8 (9, 20). The apparent decrease of the $\eta$ ratio as the energy approaches the ground state 0.48 $E_F$ (9) does not require that the local ratio $\to 0$ as $T \to 0$ because contributions from the cloud edges significantly increase S as compared with the local s at the center.

References and Notes

18. The experiments were performed far from p-wave Feinbach resonances. The relevant threshold energy for p-wave scattering was then comparable with the barrier height. Using the known $C_4$ coefficients, the barrier height for $^{40}K$ is 280 $\mu$K, whereas for $^{41}K$ the barrier height is 8 mK. Hence, for temperatures in the $\mu$K range as used in the experiments, p-wave scattering is negligible, and s-wave scattering dominates.
20. Materials and methods are available as supporting material on Science Online.

Time-Resolved Holography with Photoelectrons

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Ionization is the dominant response of atoms and molecules to intense laser fields and is at the basis of several important techniques, such as the generation of attosecond pulses that allow the determination of the electronic wavefunction in molecules.

After a strong laser field ionizes an atom or molecule, the liberated electron is accelerated by the oscillatory laser electric field and driven back toward the ion (J). Electron-ion recollision leads to the emission of extreme ultraviolet (XUV) radiation, with a duration that approaches the atomic unit of time (24.2 as) (2, 3) and encodes detailed structural and dynamical information about the atomic or molecular medium used (4–7). Alternatively, the returning electron may elastically or inelastically scatter (8, 9). These processes benefit from the 1011 A/cm2 electron recollision current incident on the target ion, exceeding current densities used in transmission electron microscopes (10). The laser-driven electron motion is fully coherent, allowing one to put into practice the concept of holography (11) and to extend it to electron-ion collisions involving laser-ionized and -driven photoelectrons (9, 12, 13). We show how under suitably chosen experimental conditions, a hologram can be recorded that encodes temporal and spatial information about both the ion (the “target”) and the recollision electron (the “source”), opening the way to a new type of ultrafast photoelectron spectroscopy of electron and nuclear dynamics in molecules.

Key to holographic electron imaging is the observation of an interference pattern between a reference wave, which is emitted from the source and does not interact with the target, and a signal wave, which scatters off the target and encodes its structure. The encoded information is stored when the signal wave interferes with the reference wave on a detector. A simple analysis borrowed from ray optics (Fig. 1A) shows that because of path length differences, a phase difference $\Delta \phi = (k - k_0)z_0$ (where $k$ is the total momentum, $k_0$ is the momentum in the $z$ direction, and $z_0$ is the distance to the scattering center) arises between the reference and scattered waves, resulting in the pattern shown in Fig. 1B.

To record a clear holographic picture, it is desirable that the reference wave not be influenced by the positively charged target and, therefore, that the electron source is located at some distance from the target, $z_0$. A suitable way to...
accomplish this is tunnel ionization in a strong low-frequency laser field, in which the electron tunnels through a barrier created by the laser field and appears at some distance from the ion.

In the presence of the laser field, the electronic wave function can be written as

$$\psi = \psi_{\text{signal}} + \psi_{\text{ref}}$$

where $\psi_{\text{signal}}$ represents a signal wave packet that oscillates in the laser field and scatters off the target and $\psi_{\text{ref}}$ represents a reference wave packet, which only experiences the laser field and does not interact with the target (14). To calculate the interference pattern produced by these two terms, we used an extension of the strong field approximation (SFA), which includes the laser field fully and the electron-ion scattering in the first Born approximation (15, 16). The result of the calculation (fig. S3A) (14) predicts that in a strong laser field, the holographic fringes remain visible and that the phase difference between the signal and the reference wave packets is

$$\Delta \phi = p_r^2 (t_c - t_0^2)/2$$

Here, $p_r$ is the momentum perpendicular to the laser polarization axis, $t_c$ is the time when the signal wave packet scatters off the ion, and $t_0^2$ is the moment of birth of the reference wave packet. Thus, the hologram can be viewed as a pump-probe experiment on the femtosecond-to-subfemtosecond time scale (fig. S3, B and C), which can encode changes in the scattering potential between $t_0^2$ and $t_c$, as well as changes in the ionization rate between $t_0^2$ and $t_0^{\text{signal}}$, which is the time of birth of the signal wave packet (14). The signal and reference wave packets that produce the holographic pattern originate from the same quarter cycle; thus, subcycle time resolution is encoded, even when long pulses are used.

A crucial aspect in our holographic imaging approach is the existence of a large electron oscillation amplitude of $a >> 1 \, \text{Å}$ and a large average oscillation energy $U_p >> \hbar \omega_{\text{laser}}$, where $\omega_{\text{laser}}$ is the laser frequency and $h$ is Planck’s constant $h$ divided by $2\pi$. In experiments with 800 nm radiation, these requirements lead to high laser intensities ($I \sim 10^{14} \, \text{W/cm}^2$) that can only be applied to ground-state atoms and molecules with a large ionization potential. To make recollision-based imaging possible at lower intensities, the laser wavelength $\lambda_{\text{laser}}$ must be increased because both $\alpha$ and $U_p$ scale as $\lambda_{\text{laser}}^{-2}$.

To demonstrate the strong-field electron holography experimentally, metastable (6 s) xenon atoms were ionized with 7-μm mid-infrared (mid-IR) radiation from the FELIX (Free Electron Laser for Intra-Cavity Experiments) beamline at the Free Electron Laser for Infrared Experiments (FELIX) facility (fig. S1)) (14, 17). The use of a large $\lambda_{\text{laser}}$ in combination with a modest ionization potential ($I P = 3.8 \, \text{eV}$) allowed the preparation of electron wave packets born at large $z_0 = IP/F_{\text{laser}}$, where $F_{\text{laser}}$ is the laser field strength, displaying a large excursion $a_\text{osc}$, without the need for a very high laser intensity ($7 \times 10^{11} \, \text{W/cm}^2$), and remaining in the tunneling regime [$(y = (2 \pi m \gamma z_0)^{1/2})/2 \, IP < 1$], where $m$ is the electron mass. Angle-resolved photoelectron spectra were recorded with a velocity map imaging spectrometer (VMIS) (18) integrated into the FELIX laser cavity. The metastable xenon atoms were exposed to a train of 5000 mid-IR laser pulses separated by 1 ns.
Varying the position of the experimental apparatus along the laser propagation axis allowed the peak intensity to be tuned by approximately a factor of five. Figure 2A to F shows a dominant electron emission along the laser polarization axis, with a high-energy cutoff (Fig. 2G) that agrees well with the classical expectation

\[ E_{\text{cutoff}} = \frac{F_{\text{laser}}^2}{2\omega_{\text{laser}}}. \]

In Fig. 3A, “side-lobes” are observed that extend from low to high momentum and run parallel to the laser polarization axis for high momenta. These side-lobes qualitatively agree with the patterns calculated in fig. S3A and result from a holographic interference. Additionally, a number of weaker transverse structures extend sideways approximately orthogonal to the laser polarization. Neither of these structures should be confused with the so-called side-lobes, “wings,” or “rings” caused by backscattered electrons that were observed in higher-order above-threshold ionization (19, 20), nor are they related to the interferences observed in recent experiments on ionization of helium by a few-cycle pulse (21).

The experimental observation of holographic interferences is confirmed through full time-dependent Schrödinger equation (TDSE) calculations, which show the same fringe pattern (Fig. 3B) (22). The fringe spacing agrees with the experiment and is reduced compared with the SFA-based calculation (fig. S3A), in which the long-range Coulomb potential was neglected.

Insight into the role of the Coulomb potential was gained by performing semiclassical calculations with the Coulomb-corrected strong-field approximation (CCSFA) (14) (23). In these calculations, complex quantum trajectories are calculated that, after tunneling, include the Coulomb interaction of the electron in the classically allowed region. The spectrum is calculated by summing contributions from different trajectories, including their phases (14). The results (Fig.
3C) quantitatively reproduce the main features discussed above. Inspection of the trajectories responsible for the side-lobes shows that these trajectories can indeed be considered as a reference and scattered wave packet, creating a hologram (Fig. 4A).

The efficiency of electron-ion recollision drops dramatically with increasing λlaser because of spreading of the wave packet between ionization and recollision. Still, a clear hologram can be observed at 7 μm. Two effects make this possible. First, the hologram results from a heterodyne experiment, in which a weaker signal is mixed with a stronger signal. Second, to create a clear reference a large-impact parameter is needed in order to limit the interaction with the Coulomb field. For large λlaser a small Dt already leads to large-impact parameters because of the long excursion time between ionization and recollision.

Inspection of the electron trajectories contributing to the transverse structures (Fig. 3) reveals that they are due to recollision events in which the scattering does not occur on the first opportunity but on the second or third (20, 24, 25). Typical examples of these trajectories are shown in Fig. 4, B to D. One, respectively two glancing electron-ion collisions can be observed before the real recollision takes place. Usually, these rare events do not leave an imprint on the photoelectron spectrum. However, the combination of a long laser wavelength and Coulomb focusing reveals that they are due to recollision events in which with increasing pressure first transforms to wadsleyite, then to ringwoodite, and then breaks down into ferropericlase and perovskite—is emblematic. These phase changes are accompanied by density and sound-velocity variations that are responsible for the main seismic discontinuities in the upper mantle (1).

In contrast, the recently discovered iron spin-state transition—where compression favors the electron spin pairing, with the system changing from a high-spin to a low-spin state—in both ferropericlase (2) and perovskite (3), the two main phases of the lower mantle, does not clearly relate to any seismic signature, although effects on mantle density and seismic wave velocity have been anticipated (4–9). In ferropericlase, the spin transition occurs without structural changes (4, 9), but experimental (10) and theoretical (11) studies suggest large softening of all the elastic moduli and, consequently, a major decrease in the aggregate sound velocities. Thus, at pressure and temperature conditions of the lower mantle, such an effect should be associated to a broad seismic anomaly (12) that, conversely, is not observed (13, 14).

Here we present inelastic x-ray scattering (IXS) measurements on \((\text{Mg}_{0.83}\text{Fe}_{0.17})\text{O}\)-ferropericlase across the spin transition and up to 70 GPa (15). We obtained the complete elastic tensor (that is, the characterization of pressure- and temperature-induced transformations in mantle minerals and their connection to seismic discontinuities aid in the understanding of Earth’s interior. In this sense, the series of phase transformations that occurs in olivine—which with increasing pressure first transforms to wadsleyite, then to ringwoodite, and then breaks down into ferropericlase and perovskite—is emblematic. These phase changes are accompanied by density and sound-velocity variations that are responsible for the main seismic discontinuities in the upper mantle (1).